

TensorRF: Tensorial Radiance Fields

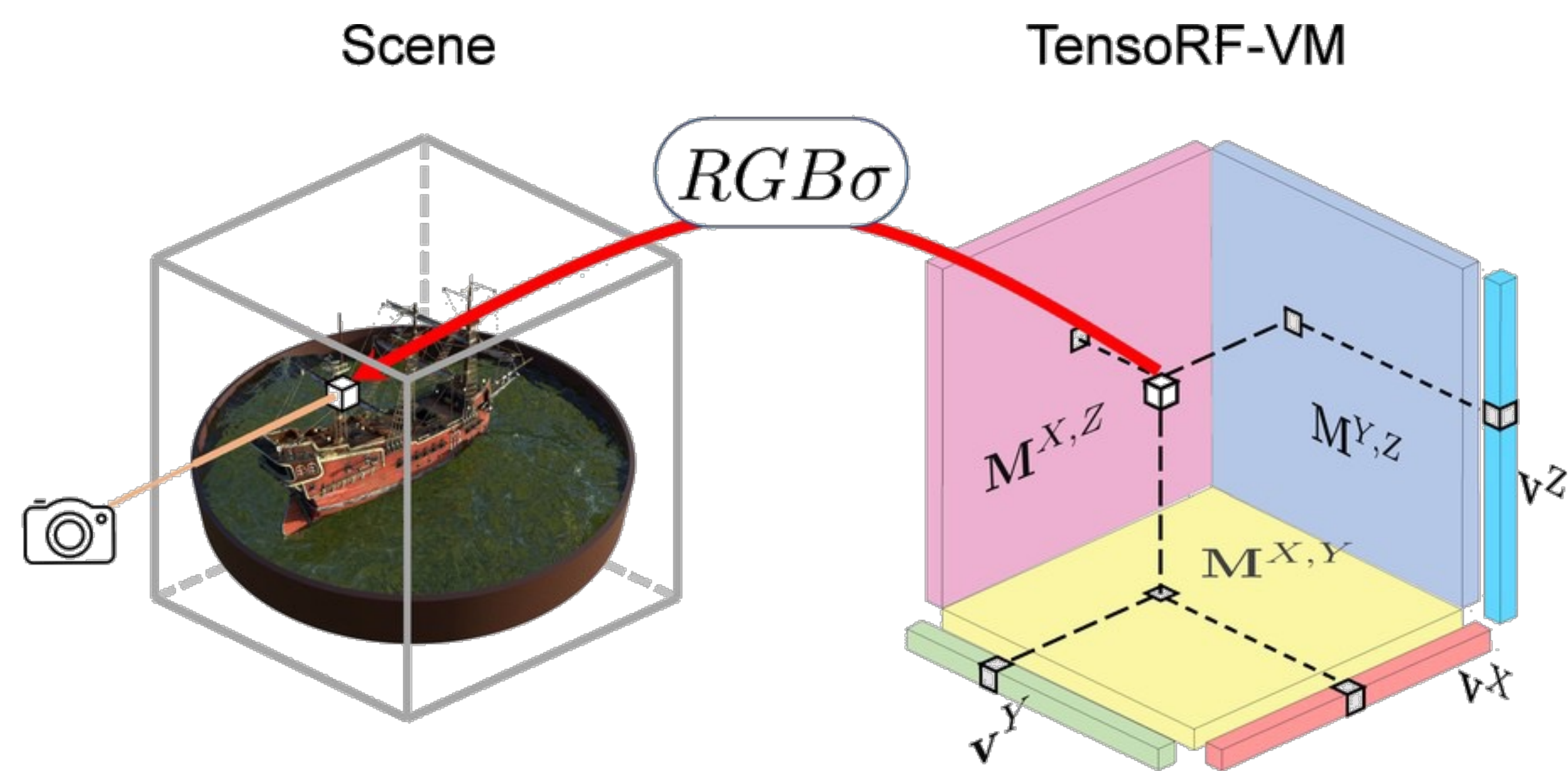
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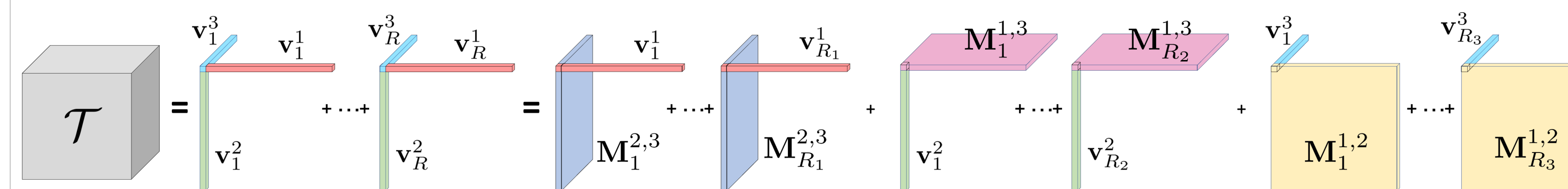
Scenes Modeling with Tensor Decomposition

We present a novel approach to model and reconstruct radiance fields. Unlike NeRF that uses pure MLPs, we consider the full volume field as a 4D tensor and propose to factorize the tensor into a set of vectors and matrices that describe scene appearance and geometry along their corresponding axes.

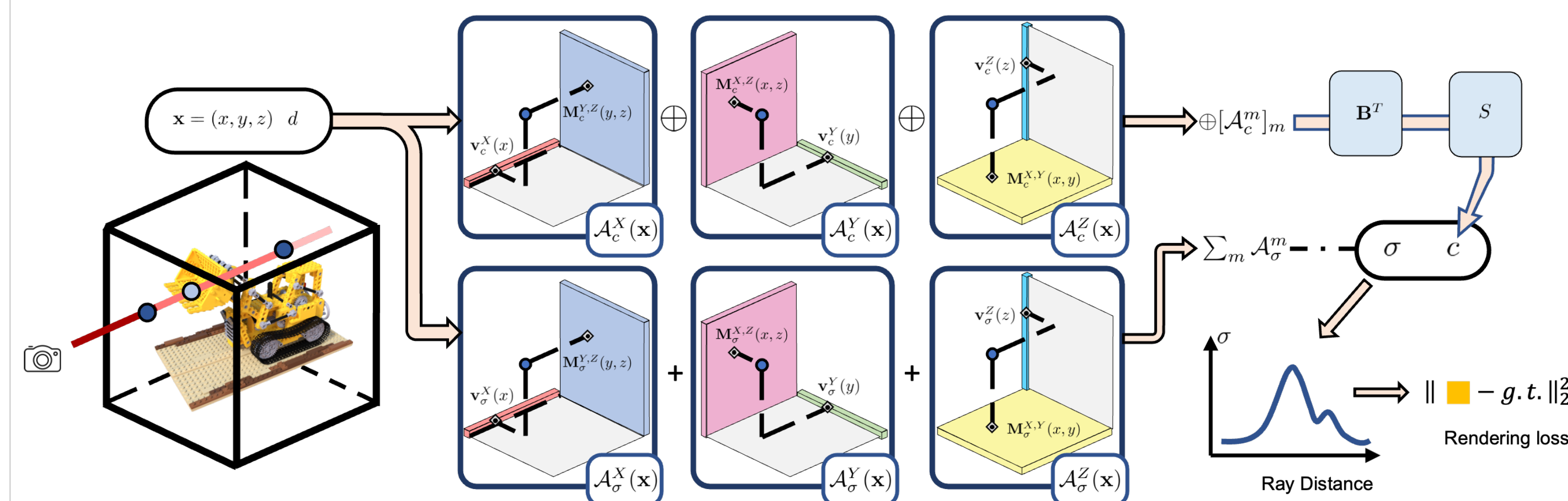


Method

We factorize radiance fields into compact components for scene modeling. To do so, we apply both the classic CP decomposition and a new vector-matrix (VM) decomposition; both are illustrated in following figure:



Left: CP decomposition, which factorizes a tensor as a sum of vector outer products. Right: our vector-matrix decomposition, which factorizes a tensor as a sum of vector-matrix outer products. Please refer to our paper for more decomposition details.



We now present our TensorRF representation and reconstruction.

For each shading location $\mathbf{x} = (x, y, z)$, we use linearly/bilinearly sampled values from the vector (\mathbf{V})/matrix (\mathbf{M}) factors to compute the corresponding trilinearly interpolated values of the tensor components.

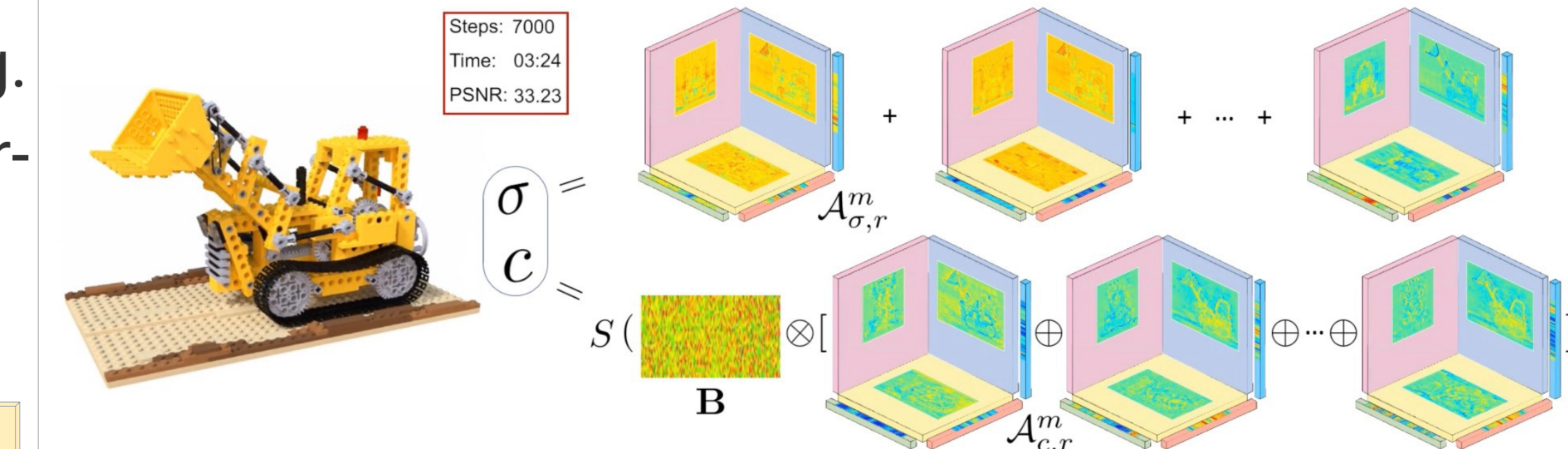
The density component values ($A_\sigma(\mathbf{x})$) are summed to get the volume density directly (σ). The appearance values ($A_c(\mathbf{x})$) are concatenated into a vector ($\oplus [A_c^m(\mathbf{x})]_m$) that is then multiplied by an appearance matrix (\mathbf{B}) and sent to the decoding function S for RGB color (c) regression.

The decoding function S can be a Spherical Harmonic (SH) function or a fully-connected network (FCN).

Table

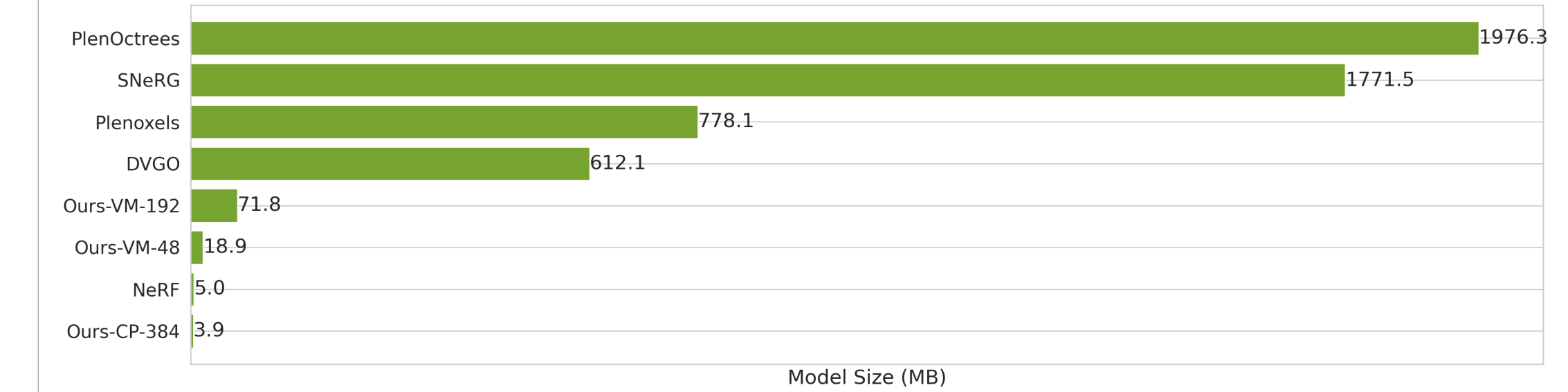
| Method | BatchSize | Steps | Synthetic-NeRF | | | | NSVF | | Tanks/Temples | | |
|------------------|-----------|-------|----------------|------------|--------|--------|--------|--------|---------------|--------|--|
| | | | Time ↓ | Size(MB) ↓ | PSNR ↑ | SSIM ↑ | PSNR ↑ | SSIM ↑ | PSNR ↑ | SSIM ↑ | |
| SRN [46] | - | - | >10h | - | 22.26 | 0.846 | 24.33 | 0.882 | 24.10 | 0.847 | |
| NSVF [26] | 8192 | 150k | >48*h | - | 31.75 | 0.953 | 35.18 | 0.979 | 28.48 | 0.901 | |
| NeRF [31] | 4096 | 300k | ~35h | 5.00 | 31.01 | 0.947 | 30.81 | 0.952 | 25.78 | 0.864 | |
| SNeRG [17] | 8192 | 250k | ~15h | 1771.5 | 30.38 | 0.950 | - | - | - | - | |
| PlenOctrees [59] | 1024 | 200k | ~15h | 1976.3 | 31.71 | 0.958 | - | - | 27.99 | 0.917 | |
| Plenoxels [43] | 5000 | 128k | 11.4m | 778.1 | 31.71 | 0.958 | - | - | 27.43 | 0.906 | |
| DVGO [47] | 5000 | 30k | 15.0m | 612.1 | 31.95 | 0.957 | 35.08 | 0.975 | 28.41 | 0.911 | |
| Ours-CP-384 | 4096 | 30k | 25.2m | 3.9 | 31.56 | 0.949 | 34.48 | 0.971 | 27.59 | 0.897 | |
| Ours-VM-192-SH | 4096 | 30k | 16.8m | 71.9 | 32.00 | 0.955 | 35.30 | 0.977 | 27.81 | 0.907 | |
| Ours-VM-48 | 4096 | 30k | 13.8m | 18.9 | 32.39 | 0.957 | 35.34 | 0.976 | 28.06 | 0.909 | |
| Ours-VM-192 | 4096 | 15k | 8.1m | 71.8 | 32.52 | 0.959 | 35.59 | 0.978 | 28.07 | 0.913 | |
| Ours-VM-192 | 4096 | 30k | 17.4m | 71.8 | 33.14 | 0.963 | 36.52 | 0.982 | 28.56 | 0.920 | |

Super Fast Convergence



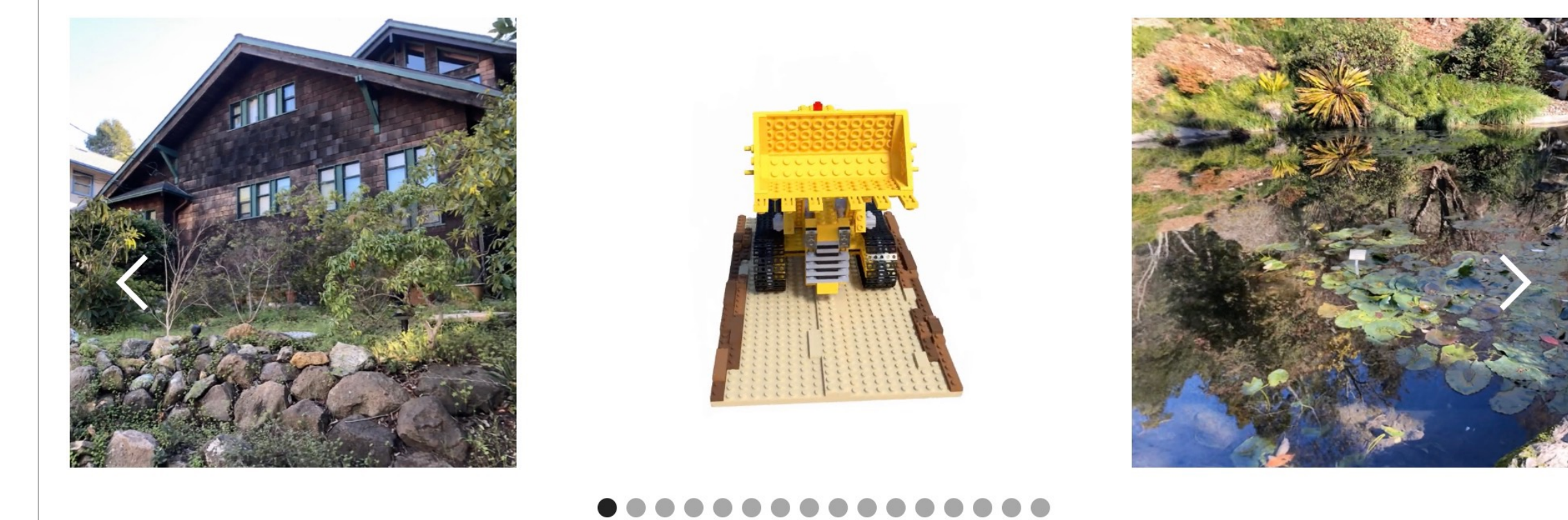
Note that, unlike concurrent works [Plenoxels](#) and [Instant-ngp](#) that require customized CUDA kernels, our model's efficiency gains are obtained using a standard PyTorch implementation.

Super Compact Memory Footprint



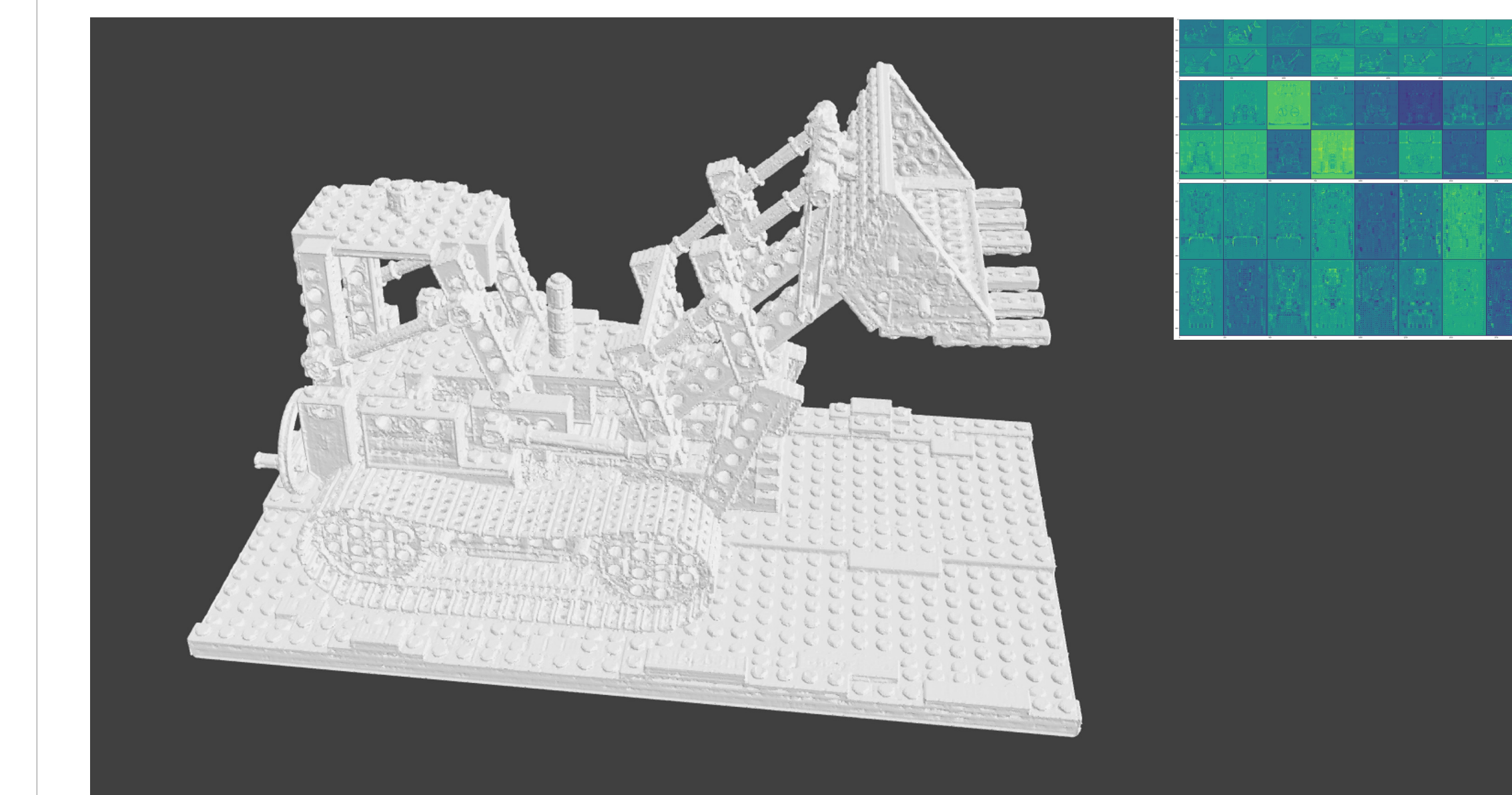
In contrast to previous works that directly reconstruct voxels, our tensor factorization reduces space complexity from $O(n^3)$ to $O(n)$ (with CP) or $O(n^2)$ (with VM), significantly lowering memory footprint.

Super Vivid Details



Our approach can also achieve high-quality radiance field reconstruction for 360° objects and forward-facing scenes.

Geometric Visualization

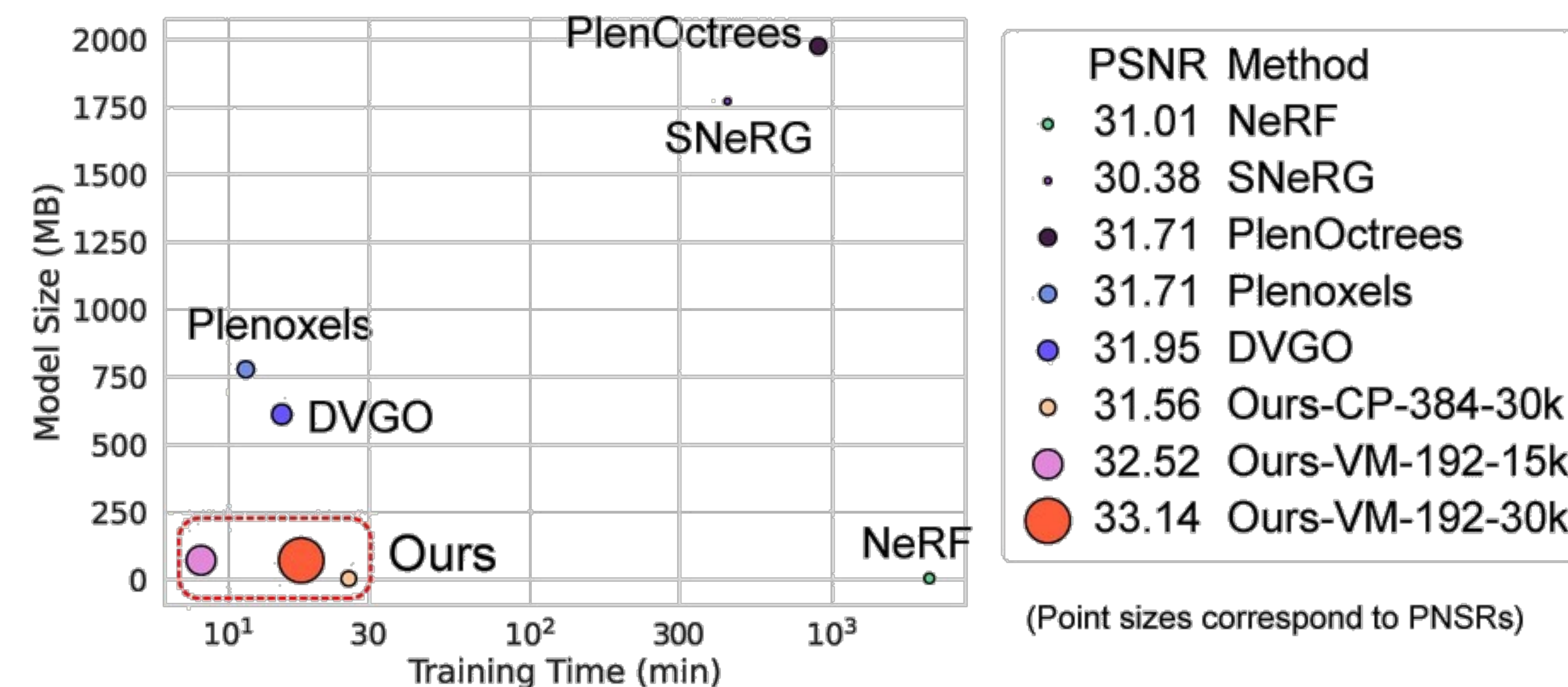


Top right: here we visualize the trained density basis of the Lego scene, the number of the basis is 16 for each dimension. We normalize the basis with min/max value along each dimension thus the brightness corresponds to their energy. We can also convert the above density basis to a mesh using marching cubes.

apchenstu.github.io/TensorRF/

Performance Overview

Quantitative Results on the Synthetic NeRF Dataset



- We demonstrate that TensorRF with CP decomposition can achieve fast reconstruction with better rendering quality and even a smaller model size (**<4MB**) than NeRF.
- Moreover, TensorRF with VM decomposition can further boost our rendering quality to outperform previous state-of-the-art methods and reduce the reconstruction time (**<10min** only with standard PyTorch implementation).